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An *italic* page number indicates that the term appears as part of an exercise in a problem section.

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